# List of data, formulae and relationships

Acceleration of free fall  $g = 9.81 \text{ m s}^{-2}$  (close to Earth's surface)

Boltzmann constant  $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$ 

Coulomb's law constant  $k = 1/4\pi\varepsilon_0$ 

 $= 8.99 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$ 

Electron charge  $e = -1.60 \times 10^{-19} \text{ C}$ 

Electron mass  $m_e = 9.11 \times 10^{-31} \text{ kg}$ 

Electronvolt  $1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$ 

Gravitational constant  $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$ 

Gravitational field strength  $g = 9.81 \text{ N kg}^{-1}$  (close to Earth's surface)

Permittivity of free space  $\varepsilon_0 = 8.85 \times 10^{-12} \, \mathrm{F m}^{-1}$ 

Planck constant  $h = 6.63 \times 10^{-34} \text{ J s}$ 

Proton mass  $m_{\rm p} = 1.67 \times 10^{-27} \, \text{kg}$ 

Speed of light in a vacuum  $c = 3.00 \times 10^8 \text{ m s}^{-1}$ 

Stefan-Boltzmann constant  $\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ 

Unified atomic mass unit  $u = 1.66 \times 10^{-27} \text{ kg}$ 

#### Unit 1

**Mechanics** 

Kinematic equations of motion  $s = \frac{(u+v)t}{2}$ 

v = u + at

 $s = ut + \frac{1}{2}at^2$ 

 $v^2 = u^2 + 2as$ 

Forces  $\Sigma F = ma$ 

 $g = \frac{F}{m}$ 

W = mg

Momentum p = mv

Moment of force moment = Fx

Work and energy  $\Delta W = F \Delta s$ 

 $E_{\rm k} = \frac{1}{2} m v^2$ 

 $\Delta E_{\rm grav} = mg\Delta h$ 

Power  $P = \frac{E}{t}$ 

 $P = \frac{W}{t}$ 

$$efficiency = \frac{useful\ energy\ output}{total\ energy\ input}$$

### Materials

Stokes' law 
$$F = 6\pi \eta rv$$

Hooke's law 
$$\Delta F = k\Delta x$$

Elastic strain energy 
$$\Delta E_{\rm el} = \frac{1}{2} F \Delta x$$

Young modulus 
$$E = \frac{\sigma}{\varepsilon}$$
 where

Stress 
$$\sigma = \frac{F}{A}$$

 $\rho = \frac{m}{V}$ 

Strain 
$$\varepsilon = \frac{\Delta x}{x}$$

### Unit 2

#### Waves

| Wave speed                             | $v = f\lambda$                          |
|--|---|
| Speed of a transverse wave on a string | $v = \sqrt{\frac{T}{\mu}}$              |
| Intensity of radiation                 | $I = \frac{P}{A}$                       |
| Refractive index                       | $n_1 \sin \theta_1 = n_2 \sin \theta_2$ |
|  | $n=\frac{c}{a}$                         |

Critical angle 
$$\sin C = \frac{1}{n}$$

Diffraction grating 
$$n\lambda = d\sin\theta$$

# **Electricity**

Potential difference 
$$V = \frac{W}{Q}$$

Resistance  $R = \frac{V}{I}$ 

Electrical power, energy  $P = VI$ 
 $P = I^2R$ 
 $P = \frac{V^2}{R}$ 
 $P = VIt$ 

Resistivity  $R = \frac{\rho l}{A}$ 

Current 
$$I = \frac{\Delta Q}{\Delta t}$$
 
$$I = nqvA$$
 Resistors in series 
$$R = R_1 + R_2 + R_3$$

Resistors in parallel 
$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

# Particle nature of light

Photon model 
$$E = hf$$

Einstein's photoelectric equation  $hf = \emptyset + \frac{1}{2}mv_{\max}^2$ 

de Broglie wavelength  $\lambda = \frac{h}{p}$ 

### Unit 4

Further mechanics

Impulse

 $F\Delta t = \Delta p$ 

Kinetic energy of a

non-relativistic particle

 $E_{k} = \frac{p^2}{2m}$ 

Motion in a circle

 $v = \omega r$ 

$$T = \frac{2\pi}{\omega}$$

$$a = \frac{v^2}{r}$$

$$a = r\omega^2$$

Centripetal force

$$F = ma = \frac{mv^2}{r}$$

$$F = mr\omega^2$$

Electric and magnetic fields

Electric field

$$E = \frac{F}{Q}$$

Coulomb's law

$$F = \frac{Q_1 Q_2}{4\pi \varepsilon_0 r^2}$$

$$E = \frac{Q}{4\pi\varepsilon_0 r^2}$$

$$E = \frac{V}{d}$$

Electrical potential

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

Capacitance

$$C = \frac{Q}{V}$$

Energy stored in capacitor

$$W = \frac{1}{2}QV$$

$$W = \frac{1}{2}CV^2$$

$$W = \frac{1}{2} \frac{Q^2}{C}$$

Capacitor discharge

$$Q = Q_0 e^{-t/RC}$$

$$I = I_0 \mathrm{e}^{-t/RC}$$

$$V = V_0 e^{-t/RC}$$

$$\ln Q = \ln Q_0 - \frac{t}{RC}$$

$$\ln I = \ln I_0 - \frac{t}{RC}$$

$$\ln V = \ln V_0 - \frac{t}{RC}$$

In a magnetic field

$$F = Bqv \sin \theta$$

$$F = BIl \sin \theta$$

Faraday's and Lenz's laws

$$\mathcal{E} = \frac{-\mathrm{d}(N\phi)}{\mathrm{d}t}$$

Nuclear and particle physics

In a magnetic field

$$r = \frac{p}{BQ}$$

Mass-energy

$$\Delta E = c^2 \Delta m$$

## Unit 5

**Thermodynamics** 

Heating 
$$\Delta E = mc\Delta\theta$$

$$\Delta E = L\Delta m$$

Ideal gas equation 
$$pV = NkT$$

Molecular kinetic theory 
$$\frac{1}{2}m < c^2 > = \frac{3}{2}kT$$

Nuclear decay

Mass-energy 
$$\Delta E = c^2 \Delta m$$

Radioactive decay 
$$A = \lambda N$$

$$\frac{\mathrm{d}N}{\mathrm{d}t} = -\lambda N$$

$$\lambda = \frac{\ln 2}{t_{1/2}}$$

$$N = N_0 e^{-\lambda t}$$

$$A = A_0 e^{-\lambda t}$$

Oscillations

Simple harmonic motion 
$$F = -kx$$

$$a = -\omega^2 x$$

$$x = A \cos \omega t$$

$$v = -A\omega \sin \omega t$$

$$a = -A\omega^2 \cos \omega t$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega}$$

$$\omega = 2\pi f$$

Simple harmonic oscillator 
$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

# Astrophysics and cosmology

Gravitational field strength 
$$g = \frac{F}{m}$$

Gravitational force 
$$F = \frac{Gm_1m_2}{r^2}$$

Gravitational field 
$$g = \frac{Gm}{r^2}$$

Gravitational potential 
$$V_{\text{grav}} = \frac{-Gm}{r}$$

Stefan-Boltzmann law 
$$L = \sigma A T^4$$

Wien's law 
$$\lambda_{\text{max}}T = 2.898 \times 10^{-3} \,\text{m K}$$

Intensity of radiation 
$$I = \frac{L}{4\pi d^2}$$

Redshift of electromagnetic 
$$z = \frac{\Delta \lambda}{\lambda} \approx \frac{\Delta f}{f} \approx \frac{v}{c}$$
 radiation

Cosmological expansion 
$$v = H_0 d$$